

ANSWER ALL THE QUESTIONS

1. Given $A = R - \{2\}$ and $B = R - \{1\}$. if $f: A \rightarrow B$ is a mapping defined by

$$f(x) = \frac{x-1}{x-2}, \text{ show that } f \text{ is bijective. Also find } f^{-1}(x). \quad [4]$$

2. If the function $f: R - \left\{\frac{7}{5}\right\} \rightarrow R - \left\{\frac{3}{5}\right\}$ be given by $f(x) = \frac{3x+4}{5x-7}$ and $g: R - \left\{\frac{3}{5}\right\} \rightarrow R - \left\{\frac{7}{5}\right\}$ be given by $g(x) = \frac{7x+4}{5x-3}$.

Show that $gof = I_A$ and $fog = I_B$, where $A = R - \left\{\frac{7}{5}\right\}$ and $B = R - \left\{\frac{3}{5}\right\}$. [4]

3. Evaluate (a) $\cos^{-1}\left(\cos \frac{13\pi}{6}\right)$ [2]

(b) $\tan\left(2\tan^{-1}\frac{1}{5} - \frac{\pi}{4}\right)$ [2]

4. Solve $\cos^{-1}x + \sin^{-1}\frac{x}{2} = \frac{\pi}{6}$. [4]

5. Evaluate $\sin^{-1}\frac{4}{5} + 2\tan^{-1}\frac{1}{3}$. [4]